

Attacks on Cryptographic Hardware

Why strong crypto is not enough

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1. The Hitchhiker's Guide to Implementation Attacks
2. Crypto, Block Ciphers and Everything
3. Mostly Harmful
4. And Another Thing ...
5. So Long, and Thanks for (all) the Keys

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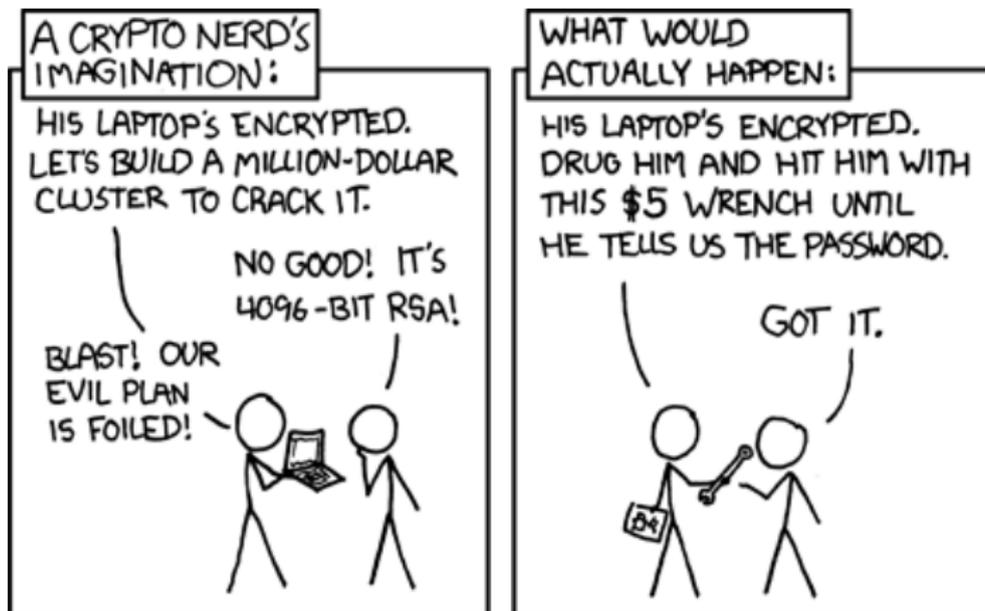


Figure: <http://xkcd.com/538>

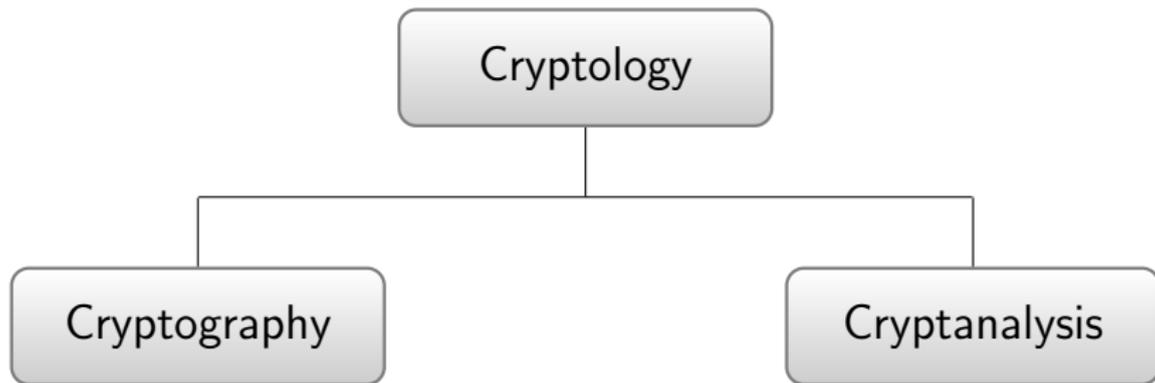


Figure: Overview of cryptology.

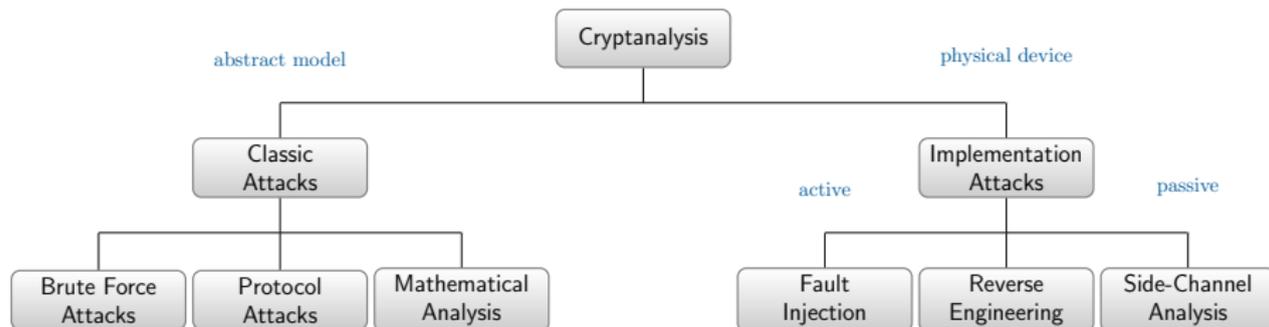


Figure: Overview of the different fields of cryptanalysis.

Definition

- ▶ An *implementation attack* is a technique where additional informations gained from the physical implementation of a cryptosystem are used during cryptanalysis.
- ▶ In other words: An attacker is not targeting directly the encryption (or decryption) map, but rather it's implementation.

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Why should we bother?

- ▶ Many fast growing fields for embedded applications: RFID, sensor networks, “Internet of Things” ...
- ▶ Areas of interest e.g. public transportation, communication, healthcare, car industry, banking sector, military.
- ▶ Drastic increase in the importance of hardware security and the demand for secure chips.
- ▶ Hardware implementing cryptographic functions (including smartcards) often show severe vulnerabilities.

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"Milking the Digital Cash Cow."

- ▶ Presented at the *29th Chaos Communication Congress* by the crypto group of the Ruhr-University Bochum.
- ▶ Extract secret keys from NXP's *Mifare DESfire MF3ICD40 smartcards* by exploiting **electro-magnetic information leakage**.
- ▶ Those cards are used e.g. for the university's "Mensacards".
- ▶ After secret key extraction: Change stored amount of money to an arbitrary value.

Further details:

- ▶ events.ccc.de/congress/2012/Fahrplan/events/5393.en.html
- ▶ www.hgi.rub.de/hgi/news/articles/milkingdigitalcashcow
- ▶ Recordings of the talk are on youtube.

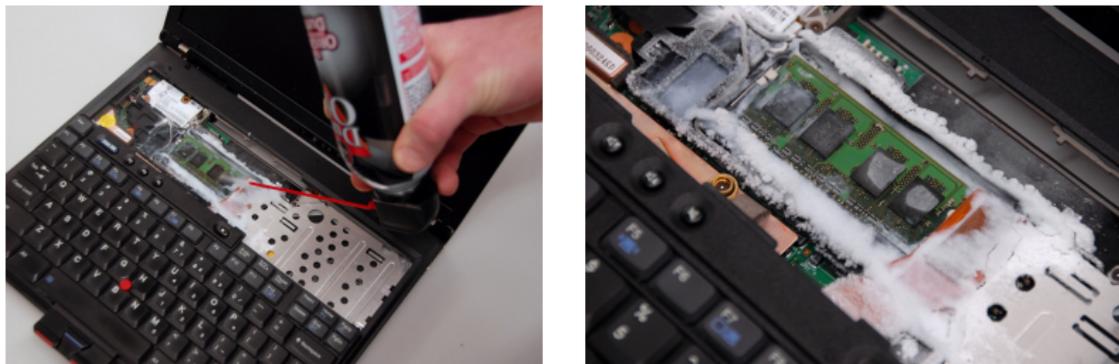


Figure: Freezing memory.

- ▶ Reconstruct full disk encryption keys from a memory dump extracted from frozen RAM.
- ▶ Further details: <https://citp.princeton.edu/research/memory>

Observation

- ▶ Power consumption of a circuit varies according to the activity of its individual components.
- ▶ Measurements of the power consumption contain informations about operations being performed and the data being processed.



Figure: Power analysis setup.

Idea: Exploit (minimal) *statistic significances* appearing in the collected power traces to extract the secret key from a device.

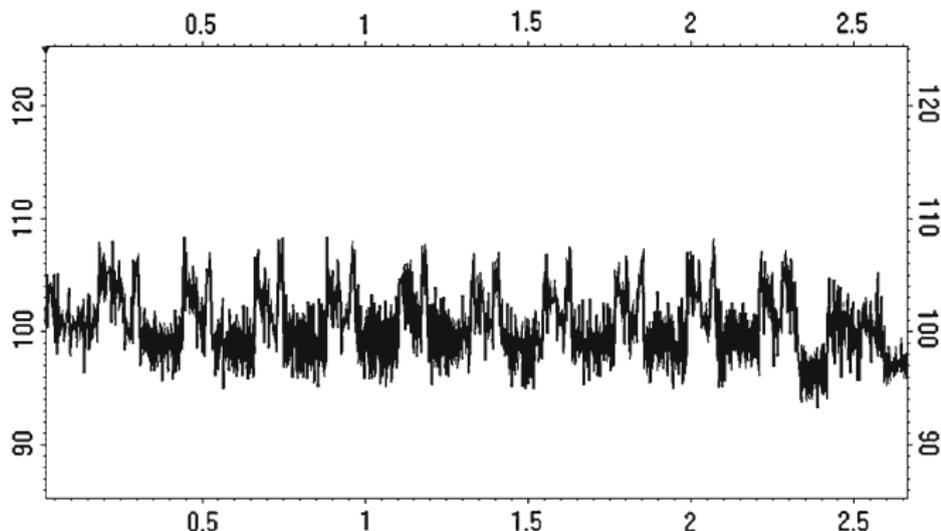


Figure: Power trace from a smart card performing an AES-128 encryption, with ten rounds clearly visible.

Some characteristics

- ▶ Attacks are **practical**, **non-invasive** and **highly effective**.
- ▶ Applicable even against complex and noisy systems where cryptographic computations account only for a small fraction of the overall power consumption.

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- ▶ By injecting faults into the electrical circuit, the attacker tries to find out something about the stored secret.
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Techniques to induce faults

- ▶ Manipulation of the power-supply voltage to cause miscalculations.
- ▶ Manipulation of the circuit's clock.
- ▶ Parasitic charge-carrier generation by a laser beam.

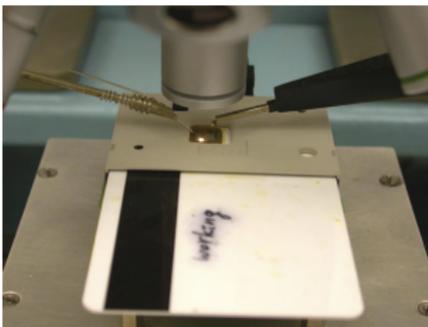


Figure: www.riscure.com

Related: Glitch attacks to break pay-tv chips or gaming consoles (PS3, XBOX).

Other types

- ▶ **Timing Analysis.**
- ▶ **Reverse Engineering:** Extraction and cryptanalysis of proprietary encryption algorithms (e.g. A5/1 stream cipher, which was used in the GSM cellular telephone standard).
- ▶ **Microprobing.**
- ▶ **Imaging.**
- ▶ **Photonic Analysis:** Measure photons that are emitted during the computations of a circuit and thereby extract secret informations.

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Don't Panic

Definition

Given a block size of n_1 bits and a key size of n_2 bits a **block cipher** is specified by an **encryption function**

$$E : \{0, 1\}^{n_1} \times \{0, 1\}^{n_2} \rightarrow \{0, 1\}^{n_1}, (m, k) \mapsto c$$

and a **decryption function**

$$D : \{0, 1\}^{n_1} \times \{0, 1\}^{n_2} \rightarrow \{0, 1\}^{n_1}, (c, k) \mapsto m$$

such that

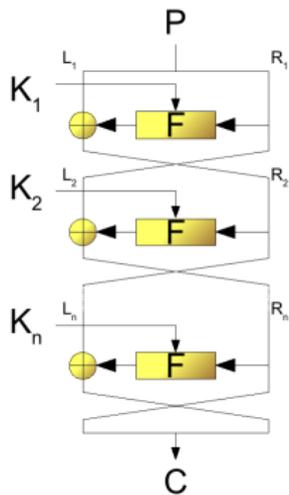
$$D_k(E_k(m)) = m$$

for all plaintext messages $m \in \{0, 1\}^{n_1}$ and all keys $k \in \{0, 1\}^{n_2}$.

Common designs

- ▶ Feistel Network
- ▶ Addition-Rotation-XOR Network (ARX)
- ▶ Substitution Permutation Network (SPN)

Overview



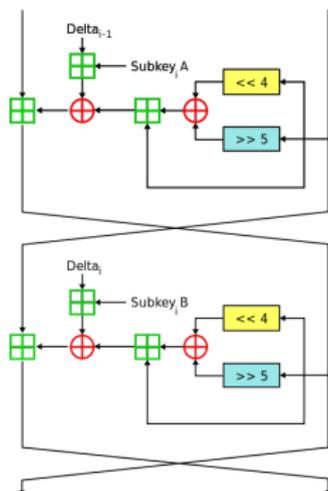
Basic procedure:

- ▶ State block splitted into: L_i, R_i
- ▶ $L_{i+1} = R_i$
- ▶ $R_{i+1} = L_i \oplus F(k_i, R_i)$

Prominent examples: DES, GOST, Blowfish, Twofish, FEAL, ...

Figure: Structure of Feistel Ciphers.

Overview



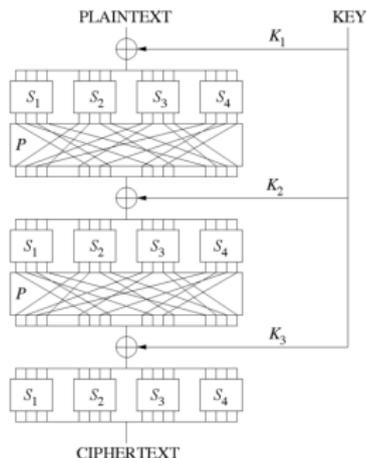
Operations:

- ▶ **Addition** (mod 2^n): \boxplus
- ▶ **Rotation**: $\lll r$
- ▶ **XOR**: \oplus

Prominent examples: RC{4,5,6}, TEA, XTEA, Threefish, ...

Figure: Example ARX Cipher: XTEA

Overview



Operations:

- ▶ Substitution: SBox application.
- ▶ Permutation.

Prominent examples: AES, PRESENT, KHAZAD, LED, PRINCE ...

Figure: Substitution Permutation Network

General features

- ▶ Uses a **64-bit state** and either a **64-bit** or a **128-bit key**, **no key schedule**.
- ▶ Number of **encryption rounds**: 32 or 48.
- ▶ Based on a Substitution-Permutation-Network (SPN).
- ▶ Design oriented on AES and PRESENT.
- ▶ Small **silicone footprint**: Especially designed for resource-constrained environments like smart cards, sensor networks etc.

(*) J. Guo, T. Peyrin, A. Poschmann and M. Robshaw, The LED Block Cipher, In: B. Preneel and T. Takagi (eds.) *CHES 2011*, LNCS, vol. **6917**, Springer, Heidelberg 2011, pp. 326–341.

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Remark

All computations are done over the finite field:

$$\mathbb{F}_{16} = \mathbb{F}_2[x]/\langle f \rangle, \text{ with } f = x^4 + x + 1$$

Notation

In the following, we represent an element $g \in \mathbb{F}_{16}$, with $g = c_3x^3 + c_2x^2 + c_1x + c_0$ and $c_i \in \mathbb{F}_2$, by

$$\phi : g \mapsto c_3 \parallel c_2 \parallel c_1 \parallel c_0$$

where \parallel denotes the concatenation of bits.

Example

The polynomial $x^3 + x + 1$ has the coefficient vector $(1, 0, 1, 1)$ and is therefore mapped to the bit string 1011 . Hexadecimal shorthand: $1011 = B$.

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The state

The 64-bit state s is considered as a concatenation of 16 4-bit strings $s_1 \parallel s_2 \parallel \dots \parallel s_{15} \parallel s_{16}$ (with $s_i \in \mathbb{F}_{16}$) and conceptually arranged in a 4×4 matrix as written below.

$$s = \begin{pmatrix} s_1 & s_2 & s_3 & s_4 \\ s_5 & s_6 & s_7 & s_8 \\ s_9 & s_{10} & s_{11} & s_{12} \\ s_{13} & s_{14} & s_{15} & s_{16} \end{pmatrix}$$

Remark

The 64-bit plaintext unit and the 64-/128-bit key are handled in the same way as the state above.

Layout

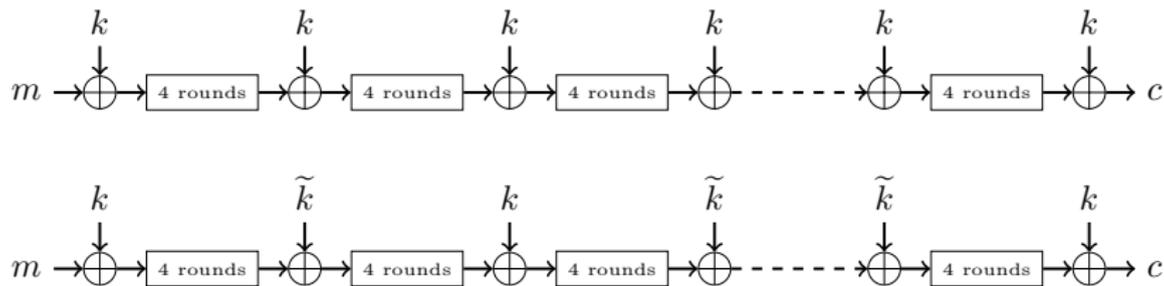


Figure: LED key usage: 64-bit key (top) and 128-bit key (bottom).

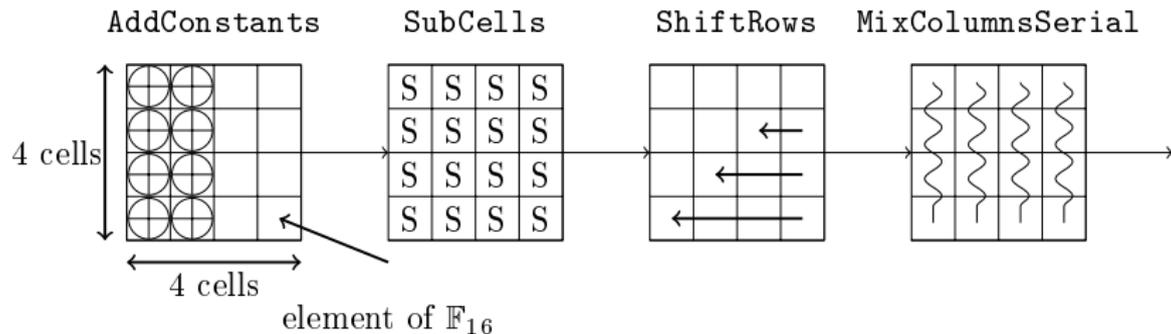


Figure: An overview of a single round of LED.

AddConstants

A **round constant** is a seq. of six bits $b_5 \parallel b_4 \parallel b_3 \parallel b_2 \parallel b_1 \parallel b_0$. Divide it into $x = b_5 \parallel b_4 \parallel b_3$ and $y = b_2 \parallel b_1 \parallel b_0$, form the matrix

$$\begin{pmatrix} 0 & x & 0 & 0 \\ 1 & y & 0 & 0 \\ 2 & x & 0 & 0 \\ 3 & y & 0 & 0 \end{pmatrix}$$

and add it to the state.

Rounds	Constants
01 – 12	01, 03, 07, 0F, 1F, 3E, 3D, 3B, 37, 2F, 1E, 3C
13 – 24	39, 33, 27, 0E, 1D, 3A, 35, 2B, 16, 2C, 18, 30
25 – 36	21, 02, 05, 0B, 17, 2E, 1C, 38, 31, 23, 06, 0D
37 – 48	1B, 36, 2D, 1A, 34, 29, 12, 24, 08, 11, 22, 04

Table: The LED round constants.

SubCells

Replace each entry x of the state matrix by the element $S[x]$ from the SBox given by the table below.

x	0	1	2	3	4	5	6	7	8	9	A	B	C	D	E	F
$S[x]$	C	5	6	B	9	0	A	D	3	E	F	8	4	7	1	2

Table: The LED SBox.

ShiftRows

For $i = 1, 2, 3, 4$, the i -th row of the state matrix is shifted cyclically to the left by $i - 1$ positions.

$$\begin{pmatrix} S_1 & S_2 & S_3 & S_4 \\ S_5 & S_6 & S_7 & S_8 \\ S_9 & S_{10} & S_{11} & S_{12} \\ S_{13} & S_{14} & S_{15} & S_{16} \end{pmatrix} \mapsto \begin{pmatrix} S_1 & S_2 & S_3 & S_4 \\ S_6 & S_7 & S_8 & S_5 \\ S_{11} & S_{12} & S_9 & S_{10} \\ S_{16} & S_{13} & S_{14} & S_{15} \end{pmatrix}$$

MixColumns

Each column v of the state matrix is replaced by the product $M \cdot v$, where M is the matrix

$$M = \begin{pmatrix} 4 & 1 & 2 & 2 \\ 8 & 6 & 5 & 6 \\ B & E & A & 9 \\ 2 & 2 & F & B \end{pmatrix}$$

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Recall

Aim: By injecting faults into the circuit during its computations, the attacker wants to gather enough informations to **reconstruct** somehow the chip's stored **secret**.

In our case



Figure: LED-64 key usage.

⇒ **Reconstruction of k .**

What are the attacker's capabilities?

- ▶ **Known plaintext attack:** We assume that the attacker is able to generate an arbitrary number of plaintext, (faulty) ciphertext triples (m, c, c') .
- ▶ **Kerckhoffs Principle** or “**The enemy knows the system**”: The **design** of the cipher is **known** to the adversary. (No security by obscurity)

Requirements

- ▶ **Temporal resolution:** Fault injection timing is controllable *quite precisely*, i.e. injection after a specific operation of the cipher.
- ▶ **Spatial resolution:** Injection effects a *single, random nibble* (4-bit value) of the whole state. The affected nibble itself is either **known** (Model 1) or **unknown** (Model 2).
- ▶ **Effects:** State nibble is changed to a *random and unknown 4-bit value*.

Note: We will focus on Model 1 in this talk.

Outline of the attack

1. **Simulate fault injection:** Add a *random, unknown fault value* to the *first entry* (or any other) of the state matrix at the beginning of the *30-th round*.
2. **Construct fault equations:** Model the relation between correct and faulty ciphertext.
3. **Filter key candidates:** Evaluation of the fault equations.
4. **Brute-force search:** On the remaining keys.

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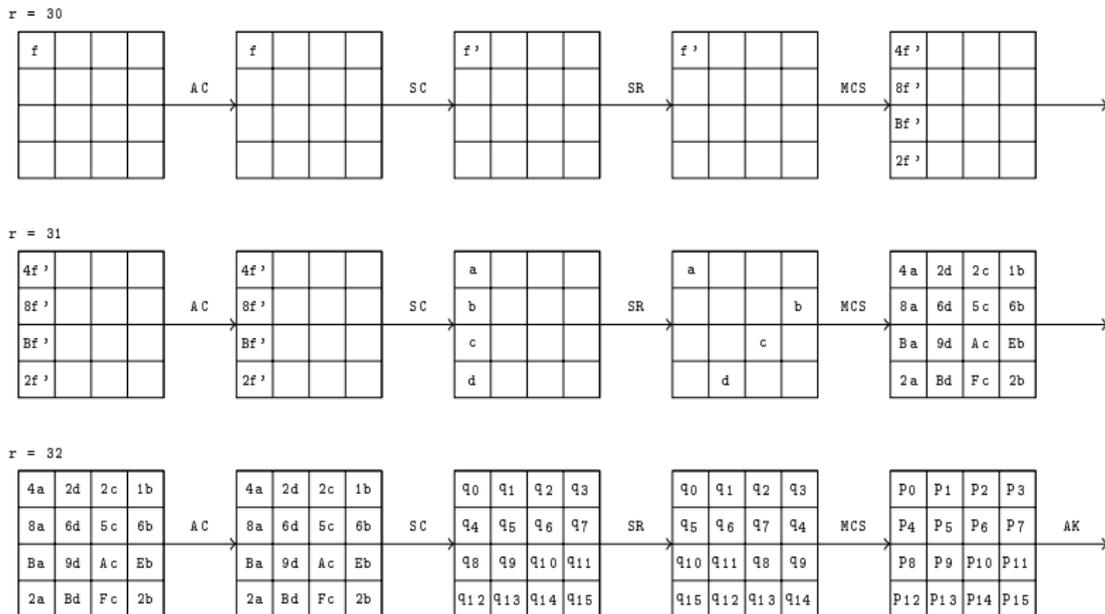
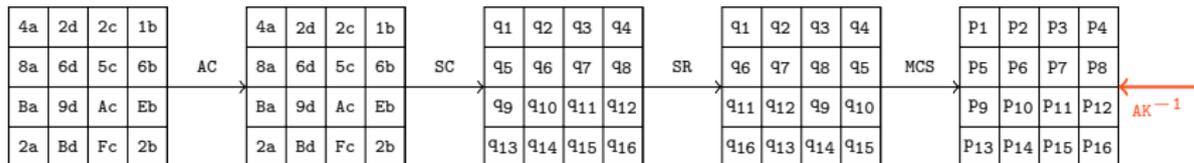


Figure: Fault propagation in the LED cipher.

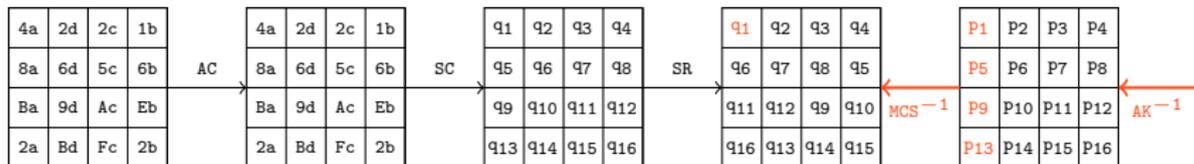
$r = 32$



Inversion of the LED steps

AK^{-1} : Compute $c_i + k_i$ and $c'_i + k_i$, for $i \in \{1, \dots, 16\}$.

$r = 32$



Inversion of the LED Steps

MCS^{-1} : Use the inverse matrix

$$M^{-1} = \begin{pmatrix} C & C & D & 4 \\ 3 & 8 & 4 & 5 \\ 7 & 6 & 2 & E \\ D & 9 & 9 & D \end{pmatrix}$$

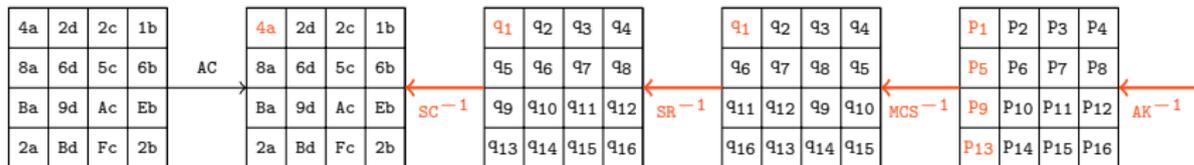
of M from the MCS operation to get:

$$C \cdot (c_1 + k_1) + C \cdot (c_5 + k_5) + D \cdot (c_9 + k_9) + 4 \cdot (c_{13} + k_{13}),$$

$$C \cdot (c'_1 + k_1) + C \cdot (c'_5 + k_5) + D \cdot (c'_9 + k_9) + 4 \cdot (c'_{13} + k_{13})$$

The other expressions are computed in a similar way.

$r = 32$



Inversion of the LED Steps

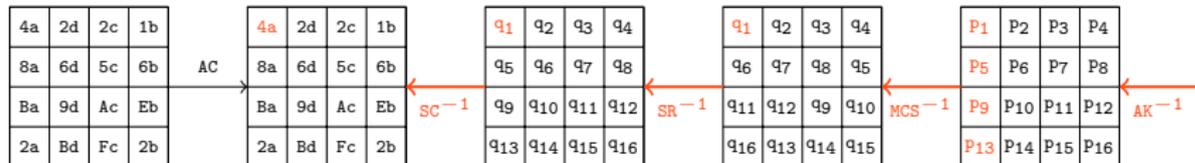
- ▶ SR^{-1} : Only shifts the entries of the state matrix, no effects on the computed expressions.
- ▶ SC^{-1} : Results in

$$S^{-1}(C \cdot (c_1 + k_1) + C \cdot (c_5 + k_5) + D \cdot (c_9 + k_9) + 4 \cdot (c_{13} + k_{13})),$$

$$S^{-1}(C \cdot (c'_1 + k_1) + C \cdot (c'_5 + k_5) + D \cdot (c'_9 + k_9) + 4 \cdot (c'_{13} + k_{13}))$$

where S^{-1} is the inverse of the LED SBox. The remaining expressions are computed in the same way again.

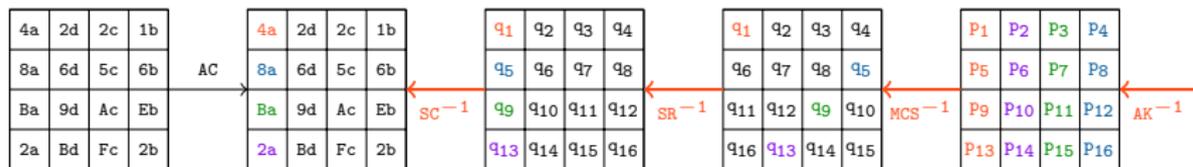
$r = 32$



Generation of the fault equations

Compute the XOR difference of two related expressions and obtain a fault equation:

$$4 \cdot a = S^{-1}(C \cdot (c_1 + k_1) + C \cdot (c_5 + k_5) + D \cdot (c_9 + k_9) + 4 \cdot (c_{13} + k_{13})) + S^{-1}(C \cdot (c'_1 + k_1) + C \cdot (c'_5 + k_5) + D \cdot (c'_9 + k_9) + 4 \cdot (c'_{13} + k_{13})).$$

$r = 32$


Fault equations for the first column

$$\begin{aligned}
 4 \cdot a &= S^{-1}(C \cdot (c_1 + k_1) + C \cdot (c_5 + k_5) + D \cdot (c_9 + k_9) + 4 \cdot (c_{13} + k_{13})) + \\
 &\quad S^{-1}(C \cdot (c'_1 + k_1) + C \cdot (c'_5 + k_5) + D \cdot (c'_9 + k_9) + 4 \cdot (c'_{13} + k_{13})) \\
 8 \cdot a &= S^{-1}(3 \cdot (c_4 + k_4) + 8 \cdot (c_8 + k_8) + 4 \cdot (c_{12} + k_{12}) + 5 \cdot (c_{16} + k_{16})) + \\
 &\quad S^{-1}(3 \cdot (c'_4 + k_4) + 8 \cdot (c'_8 + k_8) + 4 \cdot (c'_{12} + k_{12}) + 5 \cdot (c'_{16} + k_{16})) \\
 B \cdot a &= S^{-1}(7 \cdot (c_3 + k_3) + 6 \cdot (c_7 + k_7) + 2 \cdot (c_{11} + k_{11}) + E \cdot (c_{15} + k_{15})) + \\
 &\quad S^{-1}(7 \cdot (c'_3 + k_3) + 6 \cdot (c'_7 + k_7) + 2 \cdot (c'_{11} + k_{11}) + E \cdot (c'_{15} + k_{15})) \\
 2 \cdot a &= S^{-1}(D \cdot (c_2 + k_2) + 9 \cdot (c_6 + k_6) + 9 \cdot (c_{10} + k_{10}) + D \cdot (c_{14} + k_{14})) + \\
 &\quad S^{-1}(D \cdot (c'_2 + k_2) + 9 \cdot (c'_6 + k_6) + 9 \cdot (c'_{10} + k_{10}) + D \cdot (c'_{14} + k_{14}))
 \end{aligned}$$

Obtain 16 equations $E_{x,i}$ where $x \in \{a, b, c, d\}$, $i \in \{1, 2, 3, 4\}$.

Key tuple filtering (1)

- ▶ Evaluate all equations $E_{x,i}$ for all $k_l \in \mathbb{F}_{16}$ that appear in $E_{x,i}$.
Note: Every $E_{x,i}$ depends exactly on **four** key indeterminates.
(# Evaluations: $16^5 = 1048576$)

- ▶ Every evaluation produces an element $s \in \mathbb{F}_{16}$. Save the key tuple which produced s to the j -th entry of the list $S_{x,i}$ where $j = \phi(s)_{10}$.
- ▶ Determine for every $x \in \{a, b, c, d\}$ the set of possible values j_x of x such that:

$$S_{x,1}(j_x), S_{x,2}(j_x), S_{x,3}(j_x), S_{x,4}(j_x) \neq \emptyset$$

- ▶ From this obtain **fault tuples** $t = (j_a, j_b, j_c, j_d)$.

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Key tuple filtering (2)

- ▶ Compute the following intersections:

$$(k_1, k_5, k_9, k_{13}) : S_{a,1}(j_a) \cap S_{d,2}(j_d) \cap S_{c,3}(j_c) \cap S_{b,4}(j_b)$$

$$(k_2, k_6, k_{10}, k_{14}) : S_{a,4}(j_a) \cap S_{d,1}(j_d) \cap S_{c,2}(j_c) \cap S_{b,3}(j_b)$$

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- ▶ Recombine the key values (k_1, \dots, k_{16}) using all possible choices of the four intersections and get **key candidate sets**.
- ▶ Each intersection contains typically $2^4 - 2^8$ elements. Thus the size of a candidate set is usually in the range $2^{19} - 2^{26}$.

Final step: Perform a **brute force search**.

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Final step: Perform a **brute force search**.

An example

Assume we have the following setup:

$$k = 01234567 \ 89ABCDEF$$
$$m = 01234567 \ 89ABCDEF$$
$$c = FDD6FB98 \ 45F81456$$
$$c' = 51B8AB31 \ 169AC161$$

The faulty ciphertext c' was obtained by injecting the error value $e = 8$ into the first entry of the state matrix at the beginning of the 30-th round.

A Fault Attack on LED-64

a	1	2	3	4	5	6	7	8	9	A	B	C	D	E	F
#S _{a,1}	2 ¹⁴	0	2 ¹⁴	0	0	0	0	0	2 ¹⁴	0	2 ¹⁴	0	0	0	0
#S _{a,2}	0	0	0	0	0	0	0	2 ¹⁴	2 ¹⁴	0	0	2 ¹⁴	2 ¹⁴	0	0
#S _{a,3}	0	0	0	2 ¹⁴	0	0	2 ¹⁴	0	2 ¹⁴	2 ¹⁴	0	0	0	0	0
#S _{a,4}	0	2 ¹³	0	2 ¹³	0	2 ¹³	2 ¹³	2 ¹³	2 ¹⁴	0	0	0	0	0	2 ¹³

b	1	2	3	4	5	6	7	8	9	A	B	C	D	E	F
#S _{b,1}	0	0	2 ¹³	0	2 ¹³	0	0	0	2 ¹⁴	0	2 ¹³	0	2 ¹³	0	2 ¹⁴
#S _{b,2}	0	0	0	2 ¹³	2 ¹³	2 ¹⁴	0	2 ¹³	2 ¹³	0	2 ¹⁴	0	0	0	0
#S _{b,3}	2 ¹³	0	2 ¹⁴	2 ¹³	2 ¹³	0	2 ¹³	0	0	0	2 ¹³	2 ¹³	0	0	0
#S _{b,4}	2 ¹⁴	2 ¹⁴	0	0	2 ¹⁴	2 ¹⁴	0	0	0	0	0	0	0	0	0

c	1	2	3	4	5	6	7	8	9	A	B	C	D	E	F
#S _{c,1}	0	0	2 ¹⁴	2 ¹⁴	0	0	0	2 ¹³	0	0	2 ¹³	2 ¹³	0	0	2 ¹³
#S _{c,2}	2 ¹³	0	0	0	0	0	2 ¹³	2 ¹³	2 ¹³	2 ¹³	2 ¹⁴	0	2 ¹³	0	0
#S _{c,3}	2 ¹³	0	0	0	2 ¹³	2 ¹⁴	0	2 ¹⁴	0	0	2 ¹³	0	0	0	2 ¹³
#S _{c,4}	0	2 ¹³	2 ¹³	0	0	0	0	2 ¹⁴	2 ¹³	0	2 ¹³	2 ¹³	0	0	2 ¹³

d	1	2	3	4	5	6	7	8	9	A	B	C	D	E	F
#S _{d,1}	2 ¹³	2 ¹³	2 ¹³	0	0	0	2 ¹³	0	0	2 ¹³	2 ¹⁴	0	2 ¹³	0	0
#S _{d,2}	2 ¹³	2 ¹³	2 ¹³	2 ¹⁴	0	2 ¹³	0	0	0	2 ¹³	0	2 ¹³	0	0	0
#S _{d,3}	0	2 ¹⁴	2 ¹³	0	0	2 ¹³	0	2 ¹³	2 ¹³	0	2 ¹³	0	0	0	2 ¹³
#S _{d,4}	2 ¹³	2 ¹³	0	2 ¹³	0	0	2 ¹³	0	2 ¹³	2 ¹³	0	2 ¹³	0	0	2 ¹³

Results

The distribution tables give us the two fault tuples (9,5,8,2) and (9,5,B,2). This results in:

-	(9,5,8,2)	(9,5,B,2)
(k_1, k_5, k_9, k_{13})	2^7	2^6
$(k_2, k_6, k_{10}, k_{14})$	2^5	2^6
$(k_3, k_7, k_{11}, k_{15})$	2^5	2^5
$(k_4, k_8, k_{12}, k_{16})$	2^7	2^6
#keys	2^{24}	2^{23}

Observation

The key candidate sets are by construction pairwise disjoint and only one of them contains the secret key.

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#keys	2^{24}	2^{23}

Observation

The key candidate sets are by construction pairwise disjoint and only one of them contains the secret key.

Question: Can we discard candidate sets **not containing** the secret key?

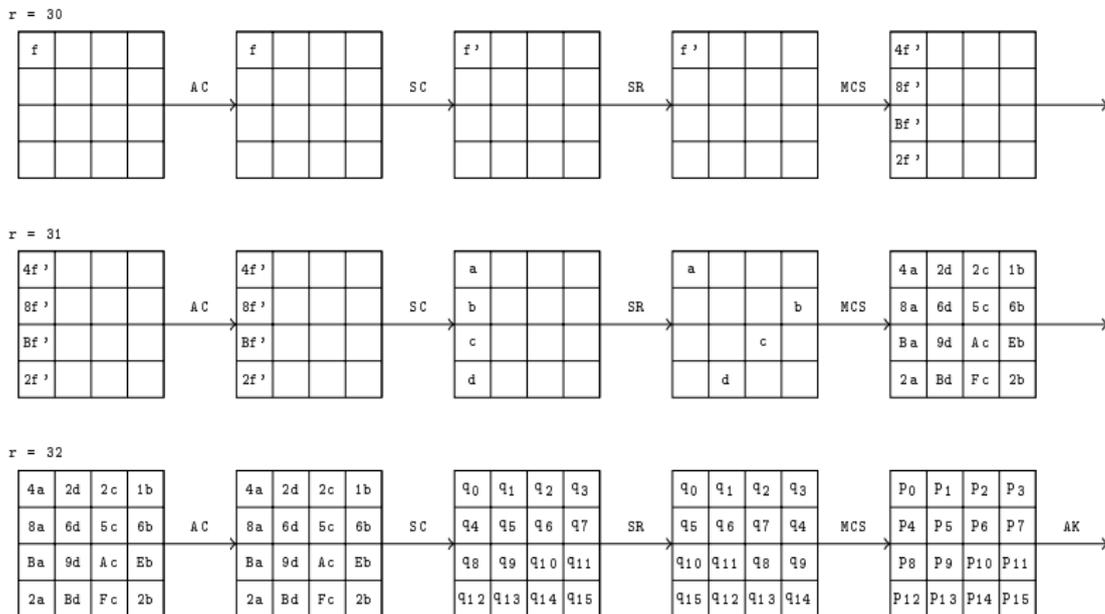


Figure: Fault propagation in the LED cipher.

Answer: Yes (in many cases) by using **key set filtering**.

Key set filtering

- ▶ One can construct the following four equations:

$$4f' = S^{-1}(y_0) + S^{-1}(y_0 + a)$$

$$8f' = S^{-1}(y_4) + S^{-1}(y_4 + b)$$

$$Bf' = S^{-1}(y_8) + S^{-1}(y_8 + c)$$

$$2f' = S^{-1}(y_{12}) + S^{-1}(y_{12} + d)$$

where $y_i \in \mathbb{F}_{16}$ are (guessed) state elements from round 31 after the SC operation was applied.

- ▶ Apply the same mechanisms as with key tuple filtering and discard all fault tuples (and thus key sets) that do not fulfill the above equations.

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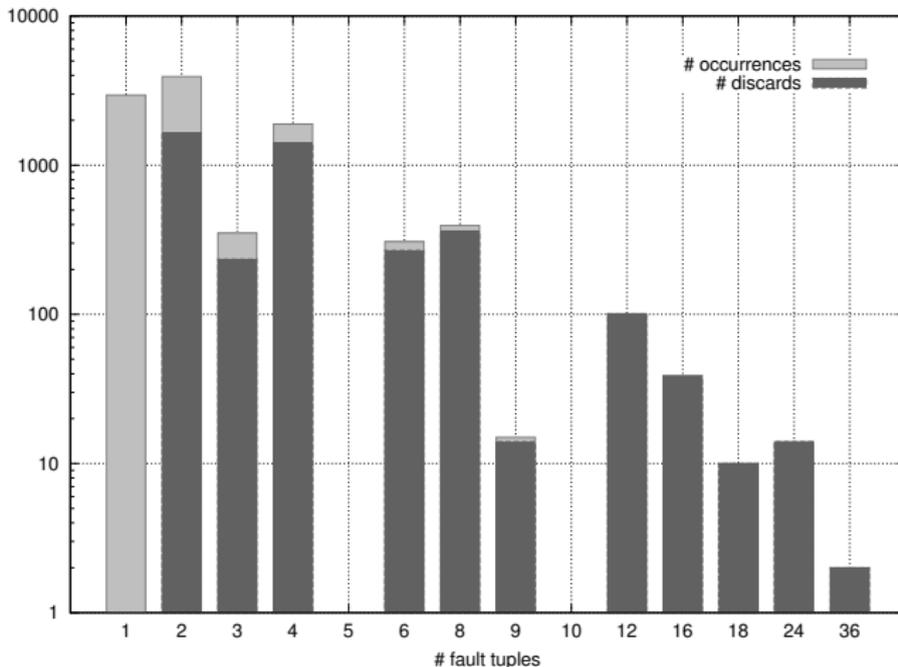
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Experimental results



Experimental results

#ft	1	2	3	4	5	6	8
occurred	2952	3926	351	1887	1	307	394
discarded	-	1640	234	1410	1	268	359
#ft	9	10	12	16	18	24	36
occurred	15	1	101	39	10	14	2
discarded	14	1	101	38	10	14	2

Table: Efficiency of key set filtering.

#ft	1	2	3	4	5	6	8
∅discarded	-	0.4	0.9	1.4	2.0	2.5	3.6
#ft	9	10	12	16	18	24	36
∅discarded	3.7	5.0	6.1	8.4	8.4	12.6	24.0

Table: Average number of discards.

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Question: Can we apply the previously described attack on LED-128, too?

Reminder: General layout of LED-64 and LED-128.

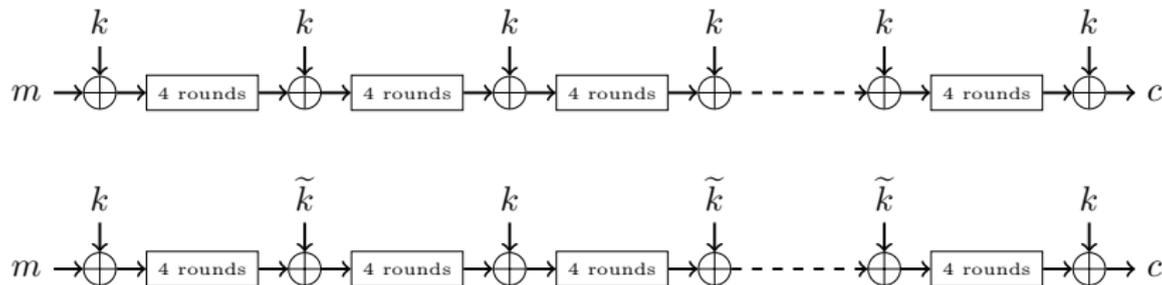


Figure: LED key usage: 64-bit key (top) and 128-bit key (bottom).

Problem with LED-128

The 64-bit keys k and \tilde{k} are not connected through some kind of key schedule and therefore independent from each other.

Reminder: General layout of LED-64 and LED-128.

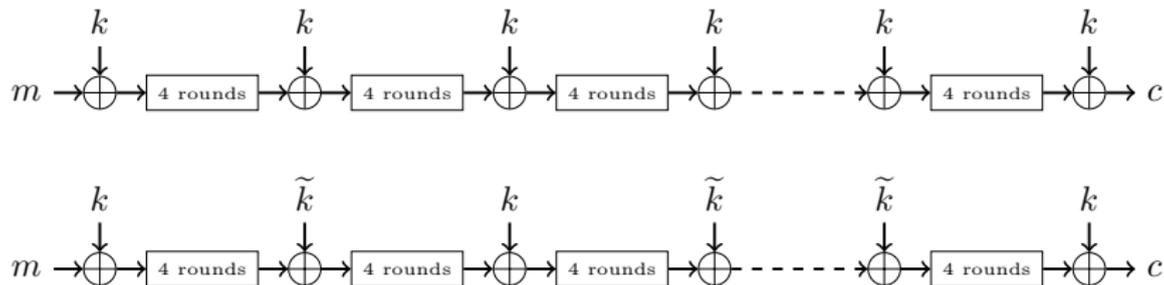


Figure: LED key usage: 64-bit key (top) and 128-bit key (bottom).

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The 64-bit keys k and \tilde{k} are not connected through some kind of key schedule and therefore **independent** from each other.

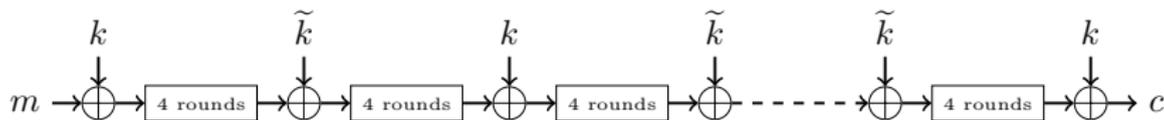


Figure: LED-128.

Outline of the attack

1. Inject a fault in **46-th round** and obtain c' . Repeat it and obtain $c'' \neq c'$.
2. Inject a fault in **42-th round** and obtain \tilde{c} .
3. Filter key candidates for k using (c, c') and (c, c'') and obtain a small number of candidates k_1, \dots, k_n ($n \leq 256$) for k .
4. Use k_i to "decrypt" the last four rounds of c and \tilde{c} , resulting in correct and faulty candidate states s_i and \tilde{s}_i .
5. Filter key candidates for \tilde{k} using (s_i, \tilde{s}_i) . Note: Many of the pairs give empty key candidate sets!
6. Perform a **brute-force search** on all the combinations of (k_i, \tilde{k}_j) .

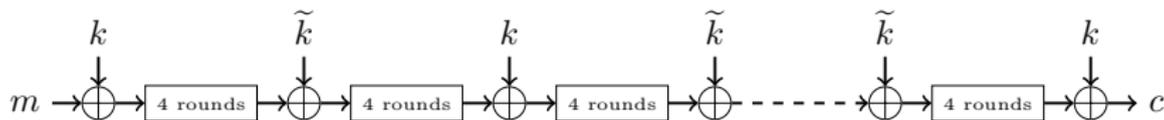


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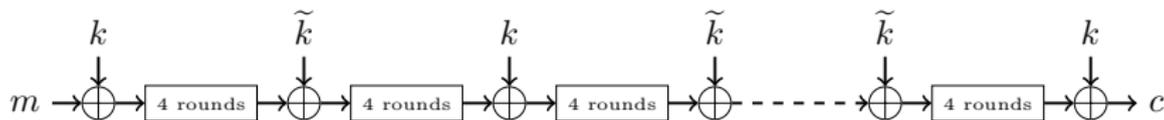


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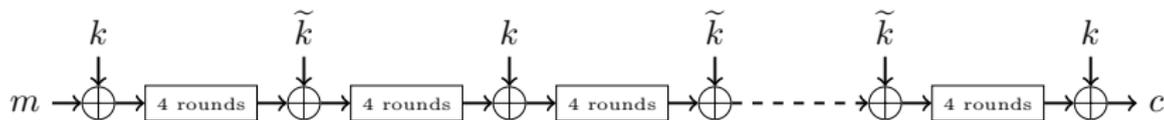


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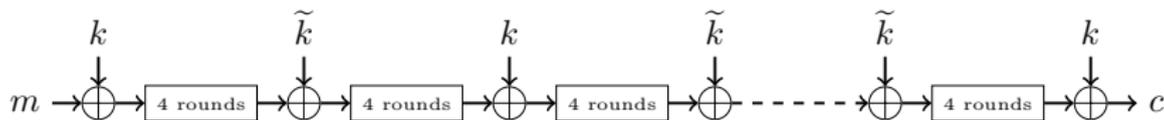


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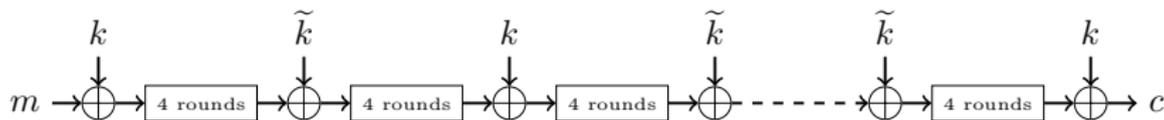
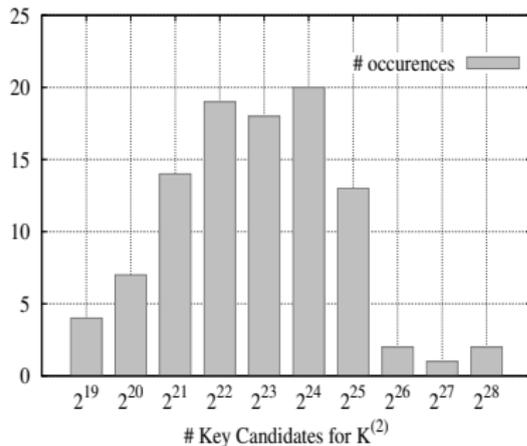
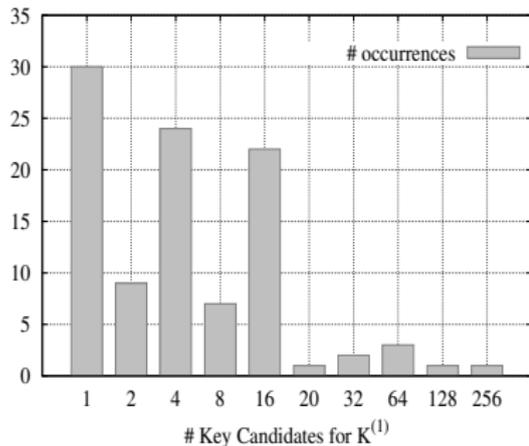


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Experimental results



- ▶ The diagrams above shows the key space sizes for 100 runs of the attack.
- ▶ The average running time for the filtering step was 517.41 seconds and 1012.51 seconds for the brute-force search.

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- ▶ Attack technologies are constantly improving and so should defensive measures.
- ▶ Designers (of hardware / software) must be aware of the latest attacks to be able to develop suitable countermeasures.
- ▶ There is no such thing as absolute protection: Given enough time and resources any protection can be broken.
- ▶ “Security is a process, not a product” - Bruce Schneier.

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What's next?

- ▶ Fault attacks on other block ciphers, stream ciphers or hash functions.
- ▶ Algebraic Fault Attacks.
- ▶ FIRE: Fault Injection for Reverse Engineering.
- ▶ ...

Interested?

- ▶ Looking for a subject for a bachelor / master thesis?
- ▶ Contact me: jovanovi@fim.uni-passau.de

Thank you for your attention!